Turbulence-Flame Interactions in Lean Premixed Dodecane Flames

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Abstract

Turbulent lean premixed *n*-dodecane/air flames are simulated in a doubly-periodic domain using detailed kinetics and transport over a range of Karlovitz number. We observe extensive thickening of thermal profiles through the flames that increases with turbulent intensity. The high Lewis number of the flames acts to suppress wrinkling of the flame resulting in considerably lower turbulent flame speeds than is observed for lower molecular weight fuels. The impact of high Lewis number is also reflected in a negative correlation of local consumption-based flame speed with curvature. Characteristic of heavy hydrocarbons, pyrolysis of the fuel into smaller fuel fragments is separated in temperature from the primary consumpution of oxygen, which peaks at a higher temperature where the fuel fragments are consumed. The resulting intermediate species are partially entrained within the cool region ahead of the flame, but the overall pyrolysis-oxidation sequence appears essentially unaffected by turbulent mixing; however, the peak rates of these reactions are dramatically reduced.

1 Introduction

Detailed chemical models for the combustion kinetics of real fuels (e.g., gasoline, diesel, and jet fuels) are important tools for improving the design of combustion technologies. A key issue in such systems is the effect of turbulent mixing on combustion chemistry, which can be explored using detailed numerical simulation. However, real fuels contain variable blends of thousands of hydrocarbon compounds so the use of detailed models is prohibitive. Instead we focus on dodecane whose molecular weight is representative of heavy practical fuels. In particular, we investigate lean premixed *n*-dodecane/air combustion in a turbulent environment using numerical simulations, based on a reduced kinetic model. There is a growing body of work of direct numerical simulation of turbulent premixed flames with detailed chemistry and transport, mostly focussing on smaller fuel molecules, such as methane and hydrogen and syngas mixtures. The goal in this work is to highlight characteristics of the chemistry-turbulence interactions specific to the pyrolysis of large-molecule fuels, and compare the oxidation and heat release of the resulting fragments to similar scenarios involving the smaller, simpler fuels.

Aspden et al. [1–4] have considered hydrogen, methane and propane flames in moderate-to-intense turbulence. Carlsson et al. [5, 6] and Tanahashi et al. [7–9] have considered turbulent premixed hydrogen and methane flames with detailed chemistry. Little work has been done on direct numerical simulation of high molecular weight hydrocarbon fuels, particularly for high Karlovitz number premixed flames. In a sequence of papers, Savard et al. [10, 11] and Lapointe et al. [12] discuss simulations of premixed heptane flames at high Karlovitz numbers with detailed chemistry and transport, building on previous work [13] based on the hydrogen simulations in [1]. The focus of these papers is on the impact of differential diffusion on flame response, even at high Karlovitz numbers; the authors note a broadening of the flame and a transition to composition versus temperature profiles characteristic of a unity Lewis number flame and a reduction in heat release and fuel consumption rates.

This paper presents simulations of lean premixed dodecane flames with detailed kinetics and transport

at high Karlovitz number, targetting matching conditions to our previous work [3, 4], and similar in spirit to the heptane simulations discussed above, but at moderate turbulence levels. Turbulent conditions are characterised in terms of the one-dimensional unstrained steady flame properties using the Karlovitz and Damköhler numbers, which are defined by

$$Ka^{2} = \frac{\check{u}^{3}}{s_{F}^{3}} \frac{l_{F}}{l} \quad \text{and} \quad Da = \frac{s_{F}}{\check{u}} \frac{l}{l_{F}}$$
 (1)

where \check{u} and l are the turbulent rms velocity fluctuation and integral length scale, respectively, and s_F and l_F are the steady unstrained flame speed and width, respectively. In the present paper, we construct cases with Ka in the range, 1–36, following the approach detailed in [1, 14]. We present an overview of the basic flame characteristics and discuss the differences between the behavior of dodecane and methane in comparable premixed turbulent flames.

2 Computational Methodology

The simulations presented here are based on a low Mach number formulation of the reacting flow equations.

The methodology treats the fluid as a mixture of perfect gases; the corresponding conservation equations for an open domain are

$$\frac{\partial(\rho \boldsymbol{u})}{\partial t} + \nabla \cdot (\rho \boldsymbol{u} \boldsymbol{u} + \tau) = -\nabla \pi + \rho \boldsymbol{F},$$

$$\frac{\partial(\rho Y_i)}{\partial t} + \nabla \cdot (\rho Y_i \boldsymbol{u} + \boldsymbol{\mathcal{F}}_i) = \rho \dot{\omega}_i,$$

$$\frac{\partial(\rho h)}{\partial t} + \nabla \cdot (\rho h \boldsymbol{u} + \boldsymbol{\mathcal{Q}}) = 0,$$

where ρ is the density, u is the velocity, h is the mass-weighted enthalpy, T is temperature. Y_i is the mass fraction and $\dot{\omega}_i$ is the molar production rate for species i. A mixture-averaged model is assumed for diffusive transport, ignoring Dufour and Soret effects; τ is the stress tensor; $\mathbf{Q} = h_i \mathbf{F}_i - \lambda \nabla T$ is the heat flux and $\mathbf{F}_i = -\rho \mathbf{D}_i \nabla X_i$ is the species diffusion. The momentum source term, \mathbf{F} , is a long-wavelength forcing

term designed to establish and maintain turbulence with the desired properties. The chemical kinetics and transport are modelled using the dodecane mechanism of You *et al.* [15], consisting of 56 species with 289 fundamental reactions. These evolution equations are supplemented by CHEMKIN-compatible databases for thermodynamic quantities. Transport properties are computing using EGLIB [16].

The basic discretisation combines a spectral deferred corrections (SDC) coupling of chemistry and transport [17] with a density-weighted approximate projection method for low Mach number flow [18]. The projection method implements a constrained evolution on the velocity field via the SDC iterations, which ensures that the update simultaneously satisfies the equation of state and discrete conservation of mass and total enthalpy. A time-explicit approach is used for advection; faster diffusion and chemistry processes are treated time-implicitly, and iteratively coupled together within the defferred corrections strategy. Since the low Mach system does not support acoustic waves, the time step size is governed by a CFL constraint based on advective transport. The integration algorithm is second-order accurate in space and time.

The performance of the numerical scheme for direct numerical simulation of premixed flame systems in regimes comparable to the present study was examined in [14]. An *effective* Kolmogorov length scale, η_{eff} , was formulated, which measures the actual Kolmogorov length scale realised in a simulation at a given resolution. Here, the most computationally demanding simulation, having the highest turbulence levels, has a computational cell width that is approximately 1.27 times the Kolmogorov length scale, η . In this case, the numerical scheme produces $\eta_{eff}/\eta < 1.03$. All other cases were better resolved.

We simulated four downward-propagating flames in a high aspect ratio domain, with periodic lateral boundary conditions, a free-slip base and outflow at the top. The momentum source term that maintains the background turbulence results in a time-dependent zero-mean velocity field. We consider four flames at atmosphere pressure with an unburned mixture temperature of 298K and an equivalence ratio of $\varphi = 0.7$. For this mixture, the freely propagating flame speed $s_F \approx 23.6$ cm/s and thermal thickness $l_F \approx 520 \,\mu\text{m}$. We note that 298K is below the boiling point of dodecane at this pressure; however, the simulations are

performed with an ideal gas equation of state that does not model condensation. The rationale for using this temperature is to facilitate comparisons with previous work on smaller fuels discussed above. As shown in [14], the turbulence forcing term gives rise to an integral length scale that is approximately one tenth of the domain size. The domain width was chosen to be $L=5.2\,\mathrm{cm}$ so that $\Lambda=lll_F=1$ and $L=10\,l=10\,l_F$. An inert calculation was run to establish the turbulence, and the reacting flow simulation was initialised by superimposing a steady unstrained flame profile onto the turbulent velocity field. Four Karlovitz numbers were chosen to match previously-reported simulations of hydrogen [3] and methane [4], which were run at $\Lambda=4$ rather than $\Lambda=1$; specifically, the four cases are $\mathrm{Ka}=1,4,12$ and 36. Note that matching simulations in hydrogen and methane at $\Lambda=1$ have also been run for comparison. The computational grid in each of the three lower Ka cases was $128\times128\times1024$, and for the $\mathrm{Ka}=36$ case was $192\times192\times1536$ to ensure that the smallest turbulence scales were sufficiently well resolved. These resolutions correspond to approximately 13 and 19 computational cells across the thermal thickness, respectively. The four cases are summarised in Table 1, and the position of these flames on the premixed regime diagram are shown in Fig. 1.

3 Results

The basic structure of the flame is illustrated with two-dimensional slices through the three-dimensional data at Ka = 36 as shown in Fig. 2. Note the extensive thickening of the density field in the preheat zone, which can also be seen in the fuel mass fraction and temperature fields, although to a lesser extent. The fuel consumption rate and heat release present much narrower profiles. As expected for a high Lewis number fuels there is a strong negative correlation between consumption rate and flame surface curvature; high reaction rates are observed where there is strong negative curvature (where the centre of curvature is in the reactants). The images of fuel consumption and heat release show a a distinct separation between where the fuel is consumed and where heat is released, which illustrates an important feature of n-dodecane combustion.

The separation of fuel consumption and heat release is indicative of a fundamental difference between combustion of dodecane and small hydrocarbons such as methane. The primary decomposition of dodecane occurs at lower temperatures through a combination of pyrolysis and oxidation reactions. Within the context of the skeletal mechanism used in this study, dodecane decomposes into a number of relatively stable intermediates, namely, CH_4 , C_2H_4 , C_3H_6 , C_4H_8 , C_5H_{10} and C_6H_{12} . The first stage of dodecane decomposition also produces pC_4H_9 and nC_3H_7 but both are highly unstable and rapidly react to form combinations of the above molecules and CH_2O , which is also stable. Images of each of these species are presented in Fig. 2. Because they are stable, they can be entrained into the cool region in front of the flame as seen in the figure.

Consumption-based global turbulent flame speeds normalised by the steady unstrained flame are presented as a function of Karlovitz number in Fig. 3, where a comparison is made with simulations of hydrogen and methane flames at the same conditions. The vertical lines indicate one standard deviation of the variation observed during this period. There are two clear trends; turbulent flame speed increases with increasing Karlovitz number and decreasing global Lewis number. For the thermodiffusively-unstable low-Lewis-number hydrogen flames, turbulence wrinkles the flame producing regions of both positive and negative curvature; positive curvature leads to a local increase in flame speed and the formation of a dominant leading edge, which is compounded by an increase in flame surface area, giving turbulent flame speeds an order of magnitude faster than the steady unstrained flame [1, 3]. For the thermodiffusively-neutral unity-Lewis-number methane flames, there is only a slight variation of local flame speed with curvature, so the enhanced flame speed results predominantly from an increase in flame surface area due to turbulence [4]. For the high-Lewis-number dodecane flames, the response to turbulence is quite different; turbulence again produces both positively and negatively curved regions. The local flame speed is enhanced in regions of negative curvature, but cannot form a leading edge in the same way as the hydrogen flames. The positively curved regions experience a defocussing of heat through diffusion, which results in a decrease in reaction rates. This decrease increases the chemical time scale, decreasing the local Damköhler number and increasing the local Karlovitz number, which makes the flame locally more susceptible to turbulent mixing; turbulence can mix partially reacted fluid into the preheat zone, which results in a pronounced thickening. The overall result on the flame speed is that it is marginally larger than that of the steady unstrained flame at low Ka and only increases by about 50% at Ka = 36.

To obtain a more quantitative measure of the curvature dependence of the flame, joint probability density functions (JPDFs) were computed of consumption-based local flame speed and flame surface mean curvature, which are presented in Fig. 4. To evaluate the local flame speed, the flame surface was identified with the 1460 K isotherm (the temperature corresponding to peak fuel consumption in the steady unstrained flame), and the fuel consumption rate was integrated in a local coordinate system constructed following temperature gradients away from the surface, following the procedure detailed in [19]. The JPDF for Ka=1 shows the negative correlation expected from a high Lewis number flame. The JPDF for Ka=36 shows a much wider range of responses and the negative correlation is less pronounced. In addition, the average consumption-based flame speed at zero curvature is considerably less than that of the steady unstrained flame; reflecting the increased chemical time scale as a result of turbulent mixing.

The impact of turbulent mixing on the flame is reflected in the thickening of the preheat zone that was illustrated in Fig. 2. To quantify the broadening of the preheat zone, a thickening factor is defined (following [4]) by taking the gradient of the temperature field, evaluating the conditional mean as a function of temperature (the conditional variable is denoted by ξ), and normalising by the corresponding profile from the Ka = 1 flame,

$$\Theta_n(T) = \frac{\langle \nabla T |_T \rangle_{Ka=1}}{\langle \nabla T |_T \rangle_{Ka=n}}$$
(2)

Note the normalisation by the Ka = 1 flame is used because the steady unstrained flame for hydrogen is not particularly relevant [20]. This choice has little effect for methane and dodecane. The thickening factors for the dodecane flames, along with the comparable results for methane and hydrogen flames, are presented in Fig. 5. For both methane and dodecane the degree of thickening increases with increasing Karlovitz number;

however, the thickening is more pronounced for dodecane - over 50% broader across most of the flame at Ka = 36. In contrast, the hydrogen flames actually get thinner, increasingly so over this range of Ka. A particularly interesting feature is the bump in the dodecane profiles, which corresponds to the temperature at peak heat release (and hence maximal gradient of temperature). We speculate that this is a signature of turbulence penetrating the reaction zone, and so the broadening of the flame at this temperature is more prounounced because of the magnitude of the temperature gradient in the reference flame.

One common feature of smaller-hydrocarbon flames exploited in experiments (e.g. [21]) is the correlation between heat release and the product of the mole fractions of OH and CH₂O. Fig. 6 presents the JPDF of heat release and $X_{OH} \times X_{CH_2O}$, which demonstrates that this correlation remains valid for dodecane combustion.

The chemical composition has been analysed through conditional means of species molar concentration conditioned on temperature. Conditional means for the primary fuel fragments are shown in Fig. 7 and other intermediate species in Fig. 8. In all cases, the black line denotes the conditional mean, and the grey regions denote one standard deviation either side of the mean. With increasing Karlovitz number, all of the primary fuel fragments generally follow the transition from the steady unstrained profile with full transport (red line) to that with unity Lewis number transport (blue line), as reported previously (see, e.g. [4]). For the intermediate species in Fig. 8, there is a departure from this behaviour. Particularly interesting is the response of molecular and atomic hydrogen; both highly mobile species. At Ka = 36, the conditional mean of molecular hydrogen has transitioned past the unity-Lewis-number profile, and the conditional mean of atomic hydrogen has moved in the opposite direction. Two species that were observed to present low-temperature activity in methane flames are HO_2 and H_2O_2 [4]; it is interesting to note that HO_2 drops below the unity Lewis number profile, while the H_2O_2 profile appears to be relatively insensitive to Ka.

To investigate the differences between combustion of dodecane combustion and smaller hydrocarbons in more detail we compare net production rates of fuel, oxidizer and key intermediates as a function of temperature in Figs. 9 and 10 for methane and dodecane, respectively. For dodecane we consider the stable intermediates discussed above. Methane oxidation begins with hydrogen abstraction to produce CH_3 . The CH_3 then reacts into three principal reaction channels. One channel represents C_2 chemistry beginning with C_2H_6 . A second channel is represent by CH_2O (with a side branch through CH_3O that then forms CH_2O). The third is a rapid transition to CH_2 through CH_2^* . For methane the fuel consumption and oxygen consumption occurs at roughly the same temperature, which is also reflected in the peak in CH_3 and CH_2 production. CH_2O and C_2H_6 are formed at cooler temperatures from radicals diffusing upstream into the cooler region of the flow. For all of these species, the net production is essentially unchanged from the laminar flame solution.

The behavior of dodecane is distinctly different. The peak in dodecane consumption occurs at around 1200K whereas the peak in O₂ consumption occurs near 1460K. Each of the key intermediates is produced where dodecane is consumed and consumed where O₂ is consumed. Furthermore, unlike methane the peak rate for each species is dramatically reduced in the turbulent case relative to the laminar flame. The response to turbulence is distinctly different than the the corresponding unity Lewis number laminar flame as indicated by the blue curve in Fig. 10. This suggests that the turbulence is beginning the disrupt the chemistry in the cool portion of the flame where the dodecane is being consumed.

4 Conclusions

Turbulent lean premixed *n*-dodecane/air flames are simulated in a doubly-periodic domain using detailed kinetics and transport over a range of Karlovitz numbers. We observe extensive thickening of thermal profiles through the flames, particularly on the cool side of the flame, and a considerable reduction in the turbulent burning speed relative to methane and hydrogen. This results from the high Lewis number of the fuel that suppresses wrinkling and leads to a negative correlation of local burning speed with curvature. Compare to methane, we find that because the fuel decomposition pyrolysis and oxidation occurs in cooler

regions of the flame, the resulting distribution of fuel fragments tends to be suseptible to mixing processes.

The basic oxidation pathways of these species is largely unaffected by this process, but the magnitudes are considerably reduced.

Several follow-on investigations are suggested by this study. Exploring the behavior with a more detailed description of dodecane combustion would be a first step. Investigation of the dodecane combustion at higher pressures characteristic of operating conditions in realistic engines would represent a longer term goal. As part of such an investigation of high-pressure flames, it would be important to investigate the impact of nonideal behavior as pressure increases.

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Case	A	В	C	D
<i>ŭ</i> [m/s]	0.226	0.570	1.18	2.47
\check{u}/s_F	1.0	2.52	5.25	10.9
Ka_F	1.0	4.0	12	36
Da_F	1.0	0.40	0.19	0.092

Table 1: Turbulence properties for the four simulations.

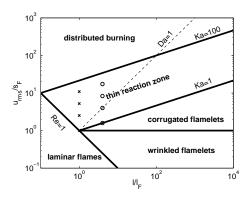


Figure 1: Regime diagram for turbulent premixed flames. The present simulations are shown by crosses, matching the Karlovitz numbers of simulations of H_2 and CH_4 in larger domains previously reported in [3, 4], which are shown by circles.

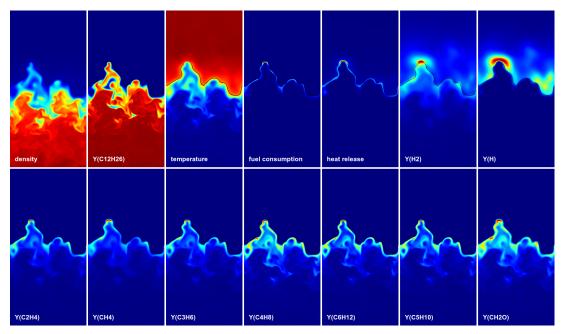


Figure 2: Two-dimensional slices through the three-dimensional data at Ka=36. Note periodicity has been exploited to stitch together x=0 and y=0 planes to show more flame surface; each panel is two domain widths across and four high. All values have been normalised by the corresponding value in the steady unstrained flame. The black contour in each field denotes the isotherm $T=1460\,\mathrm{K}$, which corresponds the temperature of peak heat release in the steady unstrained flame.

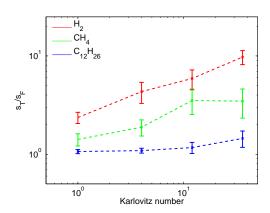


Figure 3: Consumption-based global turbulent flame speeds as a function of Karlovitz number, normalised by the steady unstrained flame speed. Crosses denote nominal averages, and the vertical lines indicate one standard deviation of the fluctuations observed once the flame has become established.

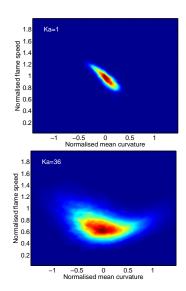


Figure 4: Joint probability density functions of normalised consumption-based turbulent flame speed s_T^c and normalised mean curvature M at $\mathrm{Ka}=1$ and 36.

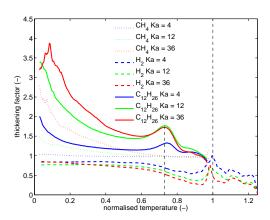


Figure 5: Thickening factor (equation 2) as a function of normalised temperature. Solid lines denote the dodecane simulations, which are compared with methane and hydrogen, represented by dotted and dashed lines, respectively. The vertical dashed line at 0.73 denotes the temperature of peak heat release in the steady unstrained flame.

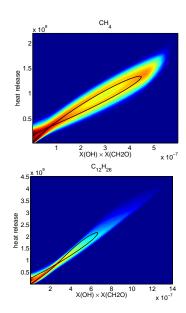


Figure 6: Joint probability density functions showing the correlation between the product of OH and CH2O mole fractions with heat release. The two cases are both at $\mathrm{Ka}=36$, with methane on the left and dodecane on the right.

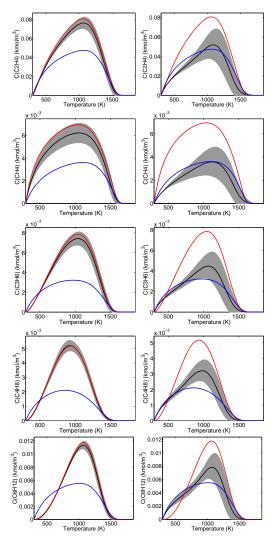


Figure 7: Conditional means of fuel fragments for $\mathrm{Ka}=1$ (left) and $\mathrm{Ka}=36$ (right). The black line denotes conditional mean, the grey area is one standard deviation either side of the mean, the red line is the steady unstrained profile, and the blue line is the unity-Lewis-number steady unstrained profile.

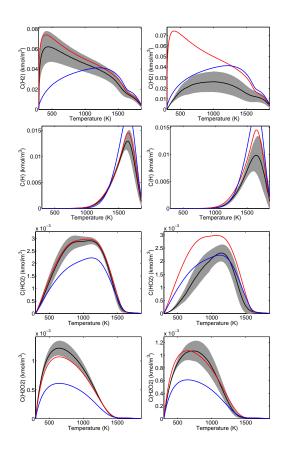


Figure 8: Conditional means of various intermediate species for $\mathrm{Ka}=1$ (left) and $\mathrm{Ka}=36$ (right); see 7 for details.

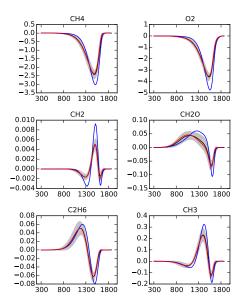


Figure 9: Conditional means of production rates ($\mathrm{Ka}=36$) for methane; ; temperature (K) vs. molar production rate (kmoles/($\mathrm{m}^3\mathrm{s}$)).

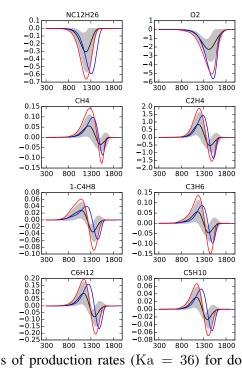


Figure 10: Conditional means of production rates (Ka = 36) for dodecane; temperature (K) vs. molar production rate (kmoles/(m^3s)).